



Question 1 [7 marks]

- (a) Derive the voltage transfer function step by step for the RC-circuit shown in Fig. 1 (a) as standard format. (4 marks)

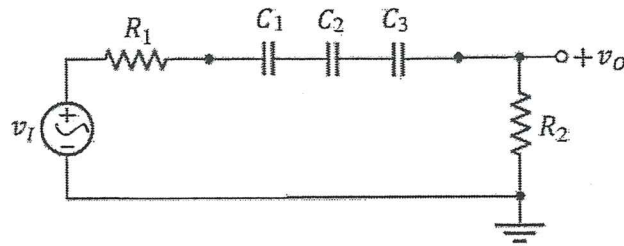


Fig. 1(a)

$\frac{1}{C_s} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$

$Z_s = R_1 + \frac{1}{sC_s}$   
 $Z_p = R_2$

$Z_s + Z_p = R_1 + R_2 + \frac{1}{sC_s} = \frac{(R_1 + R_2)sC_s + 1}{sC_s}$

$\therefore T(s) = \frac{Z_p}{Z_s + Z_p} = \frac{R_2 s C_s}{1 + s C_s (R_1 + R_2)}$   
 $= \frac{R_2}{(R_1 + R_2)} \cdot \frac{s C_s (R_1 + R_2)}{1 + s C_s (R_1 + R_2)}$   
 $= \frac{R_2}{R_1 + R_2} \cdot \frac{s \tau C_s}{1 + s \tau C_s} \quad \tau C_s = \underline{C_s (R_1 + R_2)}$

- (b) Assume that the circuit components of Fig. 1(b) are  $R_1 = 5 \text{ k}\Omega$ ,  $R_2 = 2.5 \text{ k}\Omega$ ,  $C_1 = 8 \text{ pF}$ ,  $C_2 = 5 \text{ pF}$  and  $C_3 = 15 \text{ pF}$  respectively. (3 marks)

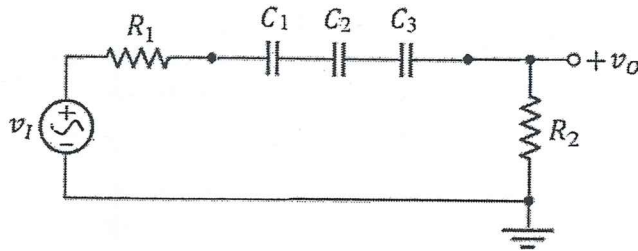


Fig. 1(b)

- i. Determine the -3dB corner frequency of the circuit
- ii. Determine the magnitude of the transfer function at -3dB corner frequency
- iii. Determine the phase of the transfer function at -3dB corner frequency

$$\frac{1}{C_s} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} \Rightarrow C_s = \frac{1}{\frac{1}{8} + \frac{1}{5} + \frac{1}{15}} = 2.553 \text{ pF}$$

$$R_{eq} = (5 + 2.5) \text{ k} = 7.5 \text{ k}$$

a) 
$$f_{3dB} = \frac{1}{2\pi R_{eq} C_s} = \frac{1}{2\pi \cdot 7.5 \text{ k} \cdot 2.553 \text{ pF}} = 8.31 \text{ MHz}$$

$$\omega_c = \frac{1}{C_s}$$

$$T(s) = \frac{R_2}{R_1 + R_2} \cdot \frac{sC}{1 + sC} = \frac{R_2}{R_1 + R_2} \cdot \frac{j\omega C}{1 + j\omega C}$$

$$|T(s)|_{\omega=\omega_c} = \frac{R_2}{R_1 + R_2} \cdot \left( \frac{1}{\sqrt{1+1}} \right)$$

$$|T(s)|_{\omega=\omega_c} = \frac{R_2}{R_1 + R_2} \cdot \frac{1}{\sqrt{2}} = \frac{2.5}{5 + 2.5} \cdot \frac{1}{\sqrt{2}} = 0.235 = -12.55 \text{ dB}$$

$$\angle \theta_{\omega=\omega_c} = (90 - 45) = 45^\circ$$

Question 2 [7 marks]

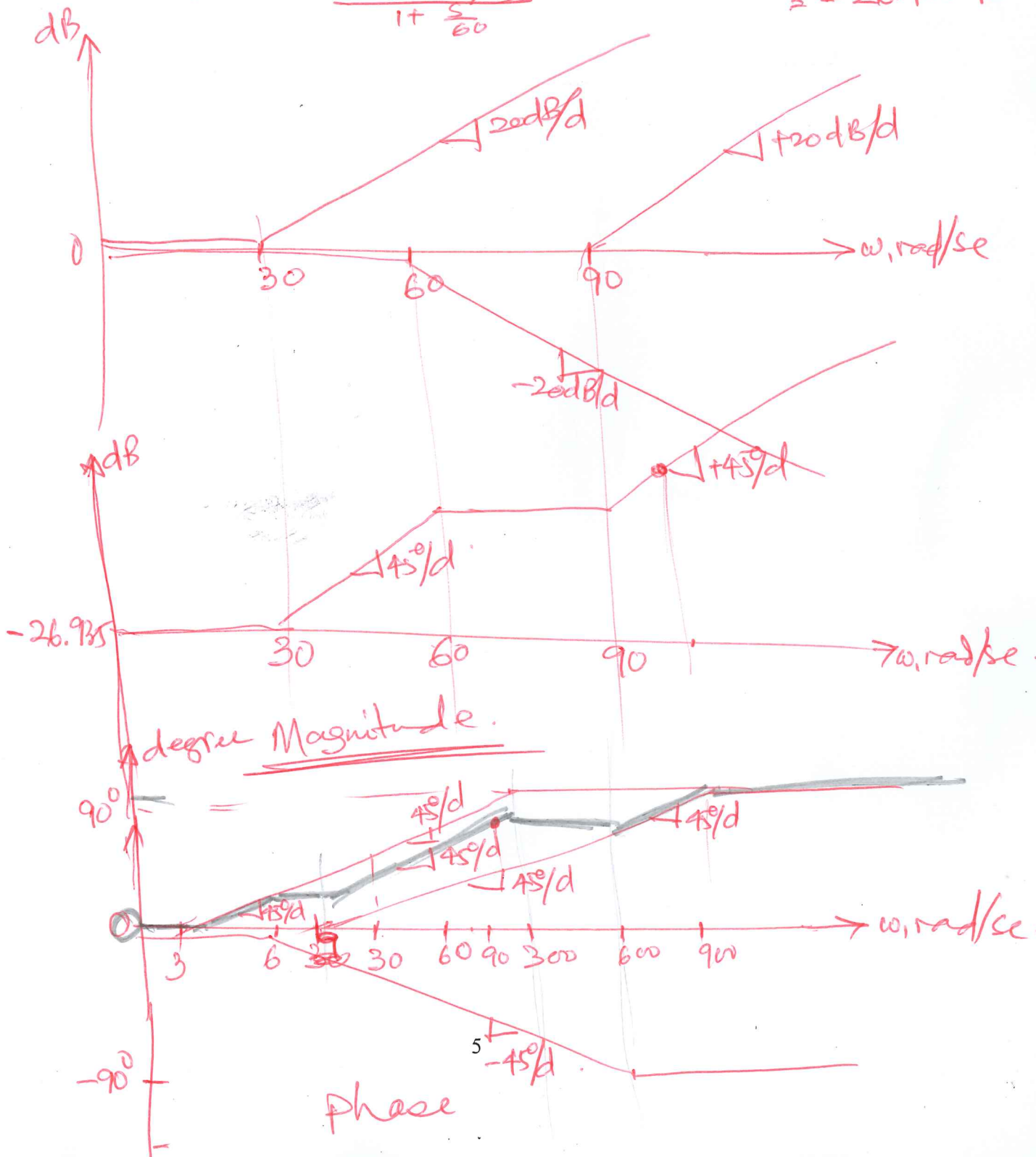
(a) Plot the Bode magnitude and phase for the following transfer function. (4 marks)

$$T(s) = \frac{10^{-3}(s + 30)(s + 90)}{(s + 60)}$$

(b) Determine the magnitude and phase at angular frequency 100 rad/sec. (3 marks)

$$T(s) = 10^{-3} \times \frac{30 \times 90}{60} \frac{\left(1 + \frac{s}{30}\right) \left(1 + \frac{s}{90}\right)}{\left(1 + \frac{s}{60}\right)}$$

$$T(s) \Big|_{dB} = 20 \log_{10} 45 \times 10^{-3} = -26.935 \text{ dB}$$



$$\omega = 100 \text{ rad/sec}$$

Magnitude

$$\left| T_{\omega, 100} \right| = 45 \times 10^{-3} \times \left| \frac{\frac{s}{30} \frac{s}{90}}{\frac{s}{60}} \right|$$

$$= \frac{45 \times 10^{-3}}{45} |s| = \frac{45 \times 10^{-3}}{45} \times 100 = 0.1$$

$$T_{dB, 100} = -20 \text{ dB} \quad \leftarrow$$

Phase:

$$\theta = \tan^{-1} \frac{\omega}{30} + \tan^{-1} \frac{\omega}{90} - \tan^{-1} \frac{\omega}{60}$$

$$= \tan^{-1} \frac{100}{30} + \tan^{-1} \frac{100}{90} - \tan^{-1} \frac{100}{60}$$

$$= 73.3 + 48.01 - 59.03$$

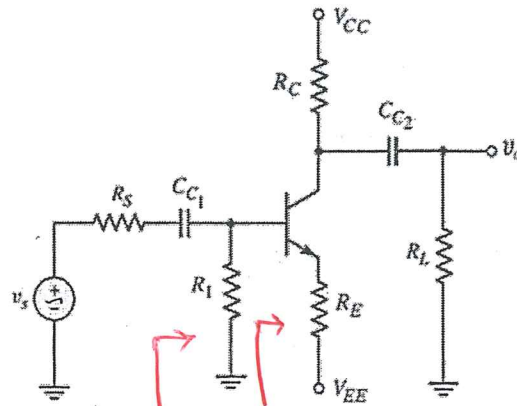
$$= 62.27^\circ \quad \leftarrow$$

**Question 3 [6 marks]**

The common emitter amplifier is shown in Fig. 3 with the following circuit component values  $R_S = 1.4 \text{ k}\Omega$ ,  $R_1 = 32 \text{ k}\Omega$ ,  $R_E = 0.5 \text{ k}\Omega$ ,  $R_C = 4 \text{ k}\Omega$ ,  $R_L = 5 \text{ k}\Omega$  and  $C_{C2} = \infty$ . The BJT has AC small-signal hybrid- $\pi$  parameters,  $g_m = 15 \text{ mA/V}$ ,  $r_\pi = 4 \text{ k}\Omega$  and  $r_o = \infty$ .

(a) Design the amplifier circuit for the lower corner frequency 2 kHz. (marks 3)

(b) Draw the small-signal equivalent circuit and determine the maximum gain of the designed amplifier in dB. (marks 3)



$\beta = 15 \times 4 = 60$

a)

$R_{ib} = r_\pi + (1 + \beta) R_E$   
 $= 4 + (1 + 60) \times 0.5 = 34.5$

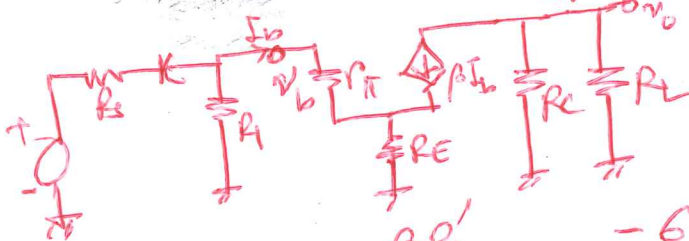
$R_i' = R_1 \parallel R_{ib} = 16.6 \text{ k}\Omega$

$f_L = \frac{1}{2\pi C_{C1} [R_S + R_i']}$

$\Rightarrow C_{C1} = \frac{1}{2\pi f_L [R_S + R_i']}$

$C_{C1} = 4.42 \text{ nF}$

b)



$R_L = 5 \parallel 4 = 2.22 \text{ k}\Omega$

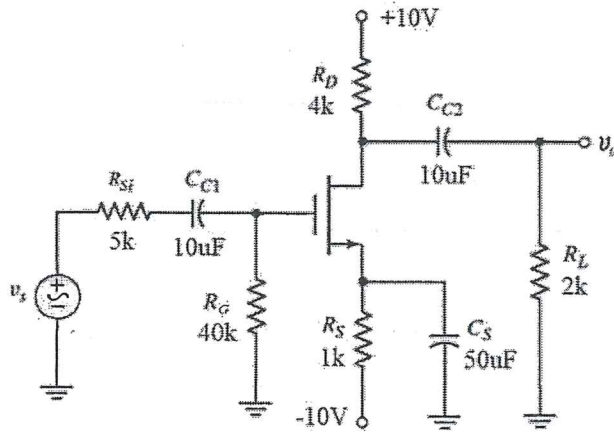
$A_{vA} = \frac{v_o}{v_b} = \frac{-\beta R_L'}{R_{ib}} = \frac{-60 \times 2.22}{34.5} = -3.865$

$A_v = A_{vA} \times \frac{R_i'}{R_i' + R_S} = -3.865 \times \frac{16.6}{16.6 + 1.4} = -3.56$

$A_v / \text{dB} = 20 \log_{10}(3.56) = 11.0391 \text{ dB}$

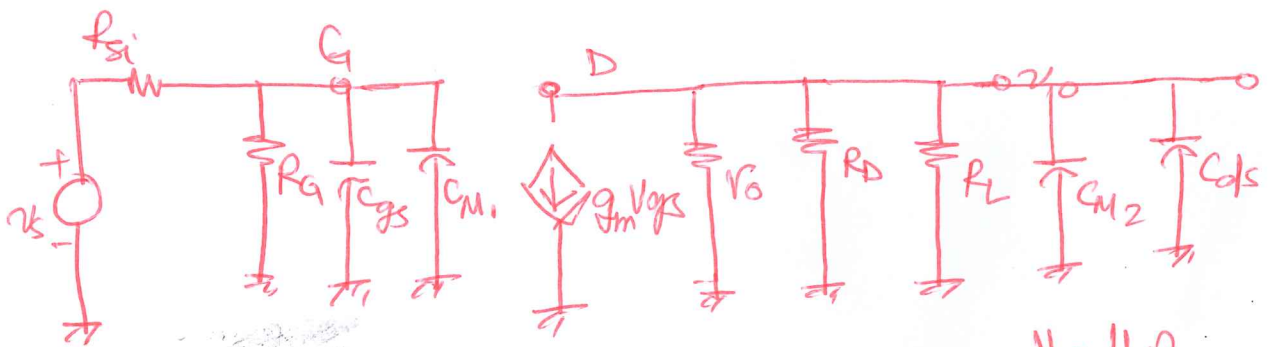
**Question 4 [5 marks]**

The common source amplifier is shown in Fig. 4. Assume that the MOSFET has small-signal high-frequency parameters,  $g_m = 20 \text{ mA/V}$ ,  $r_o = 25 \text{ k}\Omega$ ,  $C_{gs} = 12 \text{ pF}$  and  $C_{gd} = 1.5 \text{ pF}$ . Draw the Miller equivalent circuit and determine the -3dB higher corner frequency considering the miller capacitance effect. (5 marks)



$$R'_L = R_D \parallel R_L = 1.2658 \text{ k}\Omega$$

Fig. 4



$$C_{M1} = C_{gd} [1 + |A_{VA}|]$$

$$A_{VA} = \frac{-g_m v_{GS} R_D \parallel R_L}{v_{GS}} = -g_m R_D \parallel R_L = -25.316$$

$$C_{M1} = 1.5 \text{ pF} [1 + 25.316] = 39.47 \text{ pF}$$

$$C_T = C_{gs} + C_{M1} = 51.4747 \text{ pF}$$

$$R_{si} \parallel R_g = 5 \text{ k}\Omega \parallel 40 \text{ k}\Omega = 4.44 \text{ k}\Omega$$

$$f_H = \frac{1}{2\pi R_{si} \parallel R_g \times C_T} = \frac{1}{2\pi \times 4.44 \text{ k}\Omega \times 51.4747 \text{ pF}} = 695.67 \text{ kHz}$$